

# Specification of Systems with Parameterised Events: An Institution-independent Approach

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**Dedicated to Luis Soares Barbosa**

on the occasion of his 60th birthday

## Some Bits of History

- 2005: First meeting of Luis and Rolf in Macau (FACS Wsh., *Formal Aspects of Component Software*)

Common research interest: Rigorous development of reactive component systems (formal models, logics, methods)

- 2010-2013: MONDRIAN project - *Foundations for architectural design* (Luis coordinator, Rolf external consultant)
- 2015: First common publication: *Refinement in hybridised institutions*, with A. Madeira and M. Martins, FAoC journal
- 2016-2022: Continuation of our common research, with Alexander Knapp joining

## Luis' Habilitation 2016



# Development of Reactive Component Systems

We are interested in a stepwise refinement methodology

$$SP_0 \rightsquigarrow SP_1 \rightsquigarrow \dots \rightsquigarrow SP_n$$

For doing this we want a logic that is suitable for specifications of reactive component systems on various abstraction levels.

Our proposal: **Dynamic Logic with Binders**  $\mathcal{D}^\downarrow$

[ICTAC 2016] with A. Madeira and M. Martins

$\mathcal{D}^\downarrow$ -logic is suitable to express

- **abstract specifications** of requirements (safety, liveness, ...)
  - we take **regular modalities** from **Dynamic Logic**
- **constructive specifications** representing concrete processes
  - we take **variables with binders** from **Hybrid Logic**

# Actions and Formulæ in $\mathcal{D}^\downarrow$ -Logic

A **signature** is a finite set  $A$  of **atomic actions**.

**Structured actions:**

$$\alpha ::= a \in A \mid \alpha; \alpha \mid \alpha + \alpha \mid \alpha^*$$

**Formulæ:**

$$\varphi ::= \text{true} \mid \neg\varphi \mid \varphi \vee \varphi \mid \langle \alpha \rangle \varphi$$

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and  $z$  a state variable.

Usual abbreviations, like  $[\alpha]\varphi = \neg\langle \alpha \rangle \neg\varphi$

**Sentences** are formulæ without free variables.

# Semantics of $\mathcal{D}^\downarrow$ -logic

**Models are reachable LTS with initial state:**

$$\mathcal{M} = (W, w_0, (\xrightarrow{a} \subseteq W \times W)_{a \in A})$$

**Satisfaction relation:**

For sentences  $\varphi$ ,  $\mathcal{M} \models^{\mathcal{D}^\downarrow} \varphi$  if  $\mathcal{M}, w_0 \models \varphi$



## Satisfaction Relation in $\mathcal{D}^\downarrow$

For any  $A$ -model  $\mathcal{M} = (W, w_0, \rightarrow)$ ,  $w \in W$  and  $v : Z \rightarrow W$ ,

- $\mathcal{M}, w, v \models \langle \alpha \rangle \varphi$  if  
there exists  $w \xrightarrow{\alpha} w'$  such that  $\mathcal{M}, w', v \models \varphi$ ,
- $\mathcal{M}, w, v \models z$  if  $w = v(z)$ ,
- $\mathcal{M}, w, v \models \downarrow z. \varphi$  if  $\mathcal{M}, w, v\{z \mapsto w\} \models \varphi$ ,
- $\mathcal{M}, w, v \models @_z \varphi$  if  $\mathcal{M}, v(z), v \models \varphi$ ,
- ...

## Abstract and Concrete Specifications in $\mathcal{D}\downarrow$

**Example:** *Bounded Counter* with two actions *inc*, *reset*

Abstract requirements specification:

- It is always possible to reset the counter:  
 $[(inc + reset)^*] \langle reset \rangle \text{ true}$
- Whenever a reset has happened, two successive increments are possible:  
 $[(inc + reset)^*; reset] \langle inc; inc \rangle \text{ true}$
- Three increments in a row are never allowed:  
 $[(inc + reset)^*; inc; inc; inc] \text{ false}$

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Concrete specification:

- Whenever a reset has happened, the counter is in its initial state:  
 $\downarrow z_0. [(inc + reset)^*; reset] z_0$

# $\mathcal{D}^\downarrow$ -Logic is an Institution

In: [Barbosa, Hennicker, Madeira, and Martins; TCS 2018]

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- The notion of an **institution** [Goguen and Burstall 83] captures the essential ingredients that a logical system should provide when being used in formal software development.
- Clear separation between syntax (**signatures** and **sentences**), semantics (mathematical **models**) and the relationship between the two in terms of **satisfaction relations**  $M \models_\Sigma \varphi$ .

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An **institution** consists of

- a category *Sig* of *signatures*,
- a *sentences* functor  $\text{Sen} : \text{Sig} \rightarrow \text{Set}$ ,
- a *models* functor  $\text{Mod} : \text{Sig}^{\text{op}} \rightarrow \text{Cat}$ , and
- a family of **satisfaction relations**  $\models_\Sigma \subseteq |\text{Mod}(\Sigma)| \times \text{Sen}(\Sigma)$

such that the *satisfaction condition* holds, i.e.

for all  $\sigma : \Sigma \rightarrow \Sigma'$  in *Sig*,  $M' \in \text{Mod}(\Sigma')$ , and  $\varphi \in \text{Sen}(\Sigma)$

$$\text{Mod}(\sigma)(M') \models_\Sigma \varphi \iff M' \models_{\Sigma'} \text{Sen}(\sigma)(\varphi)$$

# Integrating Data: The Event/Data-Based Logic $\mathcal{E}^\downarrow$

**Example:** *Bounded Counter*

with two **data attributes**  $val : \text{Nat}$ ,  $max : \text{Nat}$

Abstract requirement:

Whenever the counter value is smaller than the upper bound an increment is possible:

$$[(inc + reset)^*](val < max) \rightarrow \langle inc // val' = val + 1 \rangle \text{true}$$

## Syntactic Concepts of $\mathcal{E}^\downarrow$ -Logic

An **event/data signature**  $\Sigma = (E, \Delta)$  consists of a finite set  $E$  of **events** and a finite set  $\Delta$  of **data attributes**.

**Event/data actions:**

$$\alpha ::= e // \psi_{2\Delta} \mid \alpha; \alpha \mid \alpha + \alpha \mid \alpha^*$$

where  $e \in E$  and  $\psi_{2\Delta}$  is a “2-data state formula”,  
i.e. a data state formula over  $\Delta \cup \Delta'$ .

**$\Sigma$ -formulae:**

$$\varphi ::= \text{true} \mid \neg\varphi \mid \varphi \vee \varphi \mid \langle \alpha \rangle \varphi \mid z \mid \downarrow z. \varphi \mid @_z \varphi \mid \psi_\Delta$$

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**We can turn  $\mathcal{E}^\downarrow$ -logic into an institution**

In: [Hennicker, Knapp, Madeira; FAoC 2021]

*Hybrid dynamic logic institutions for event/data-based systems*

# Integrating Event Parameters

Submitted for [Festschrift for Luis, 2022]

## **Example:** *Bounded Counter*

Event with parameter:  $inc(x)$  where  $x$  is a variable of type  $\text{Nat}$ .

Let  $\varphi$  be:  $\forall x. (val + x \leq \max \rightarrow \langle inc(x) // val' = val + x \rangle \text{true})$

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$\mathbf{any} x$  expresses a non-deterministic choice for the value of  $x$

## Structured Actions and Formulæ in $\mathcal{E}_p^\downarrow$ -Logic

An **event/data signature**  $\Sigma = (E, \delta)$  consists of

- a finite set  $E$  of **parameterised events**  $e(\mathbf{any} X)$  where  $X$  is a finite list of variables and
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The **set of event/data actions** over  $\Sigma$  is given by

$$\alpha ::= e(\mathbf{any} X) // \psi_{2\delta}(Y) \mid \alpha; \alpha \mid \alpha + \alpha \mid \alpha^*$$

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## Our Solution Reconsidered

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But  $inc(x) \langle \dots \rangle$  is not syntactically correct.

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$\forall x. (val + x \leq max \rightarrow \langle inc(x) \parallel val' = val + x \rangle true)$

But  $inc(x) \parallel \dots$  is not syntactically correct.

Therefore we write

$[(inc(\mathbf{any} x) + reset)^*]$

$\forall x. (val + x \leq max \rightarrow \langle inc(\mathbf{any} y) \parallel y = x \wedge val' = val + x \rangle true)$



## Open Formulæ and Valuations (institution independent)

Let  $\delta : \Delta_0 \rightarrow \Delta$  be a data signature morphism.

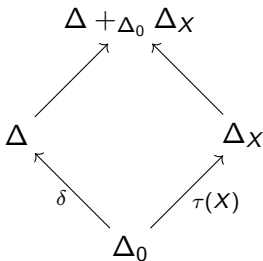
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An **open  $\delta$ -formula** is a pair, written  $\varphi(X)$ , such that  $X$  is a finite set of variable names and  $\varphi$  is a data sentence over the pushout signature

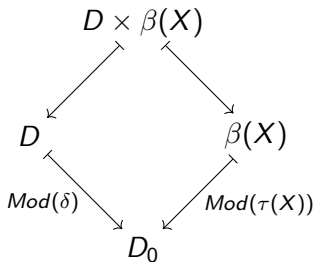


A **valuation** for the variables  $X$  is a function  $\beta$  which maps any  $x \in X$  to a  $\Delta_x$ -data model  $\beta(x)$ .

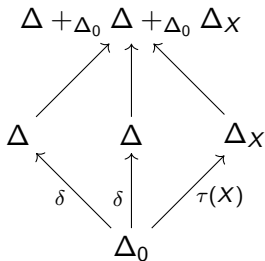
## Satisfaction of Open Data Formulæ

For  $\delta : \Delta_0 \rightarrow \Delta$  we assume a fixed  $\Delta_0$ -model  $D_0$  and we consider the class of  $\Delta$ -models  $D$  whose reduct along  $\delta$  is  $D_0$ .

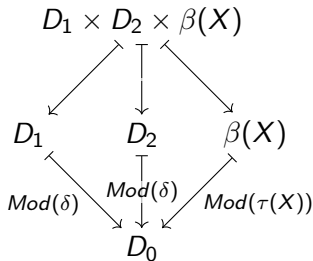
We define:  $D, \beta \models_{\delta} \varphi(X)$  if  $D \times \beta(X) \models_{\Delta + \Delta_0 \Delta_X} \varphi$



## Dealing with Open 2-Data State Formulae



(a) Colimit



(b) Limit

We define:

$(D_1, D_2), \beta \models_{2\delta} \psi(X)$  if  $D_1 \times D_2 \times \beta(X) \models_{\Delta + \Delta_0 \Delta + \Delta_0 \Delta_X} \psi$

e.g.  $\psi(\{x\}) \equiv (\text{val}' = \text{val} + x)$

## Semantic Models in $\mathcal{E}_p^\downarrow$

Let  $\Sigma = (E, \delta : \Delta_0 \rightarrow \Delta)$  be an event/data signature.

A **configuration** is a pair  $\gamma = (ctrl, data)$  where *ctrl* is a **control state** and *data* is a **data state** formalised as a model over the data signature  $\Delta$  (whose reduct along  $\delta$  is  $D_0$ ).

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A  **$\Sigma$ -model** is a labelled transition system  $\mathcal{M} = (\Gamma, \gamma_0, \rightarrow)$  such that

- $\Gamma$  is a *set of configurations*,
- $\gamma_0 \in \Gamma$  is the *initial configuration*,
- $\rightarrow$  is a family of *transition relations*  $\xrightarrow{e(\beta_X)} \subseteq \Gamma \times \Gamma$ , one for each event  $e(\text{any } X) \in E$  and each valuation  $\beta_X$  for  $X$ ,
- all configurations in  $\Gamma$  are reachable from  $\gamma_0$  via  $\rightarrow$ .

## Satisfaction Relation in $\mathcal{E}_p^\downarrow$

For any  $\Sigma$ -model  $\mathcal{M}$ , configuration  $\gamma \in \Gamma$  and data variable valuation  $\beta : \mathcal{X} \rightarrow \text{Mod}(\delta)$  “data models”,

- $\mathcal{M}, \gamma, \beta \models \langle e(\text{any } X) \parallel \psi_{2\delta}(Y) \rangle \varphi$  if

there exists a valuation  $\beta_X$  for  $X$  and  $\gamma \xrightarrow{e(\beta_X)} \gamma'$  such that

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*Related work:* [Martins, Madeira, Diaconescu, Barbosa; CALCO 2011]  
*Hybridization of institutions*

## Conclusion

**Let us celebrate Luis!**

With all our best wishes for  
many further happy and successful years!

